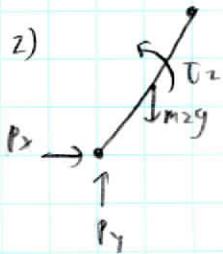
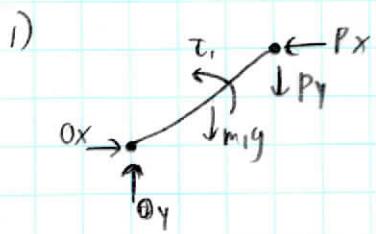


• Separate each link into a FBD



$$(1) \quad \sum F_y = m_1 a_{y1} = \ddot{\theta}_1 - m_1 g - P_y$$

$$\sum F_x = m_1 a_{x1} = P_x - \ddot{\theta}_1$$

$$\sum M_O = I_1 \ddot{\theta}_1 = \tau_1 - m_1 g \frac{l_1}{2} \cos(\theta_1) - P_y l_1 \cos(\theta_1) + P_x l_1 \sin(\theta_1)$$

$$(2) \quad \sum F_y = m_2 a_{y2} = P_y - m_2 g \quad \ddot{a}_y = \ddot{y}, \quad \ddot{a}_x = \ddot{x}, \quad \ddot{\alpha} = \ddot{\theta}$$

$$\sum F_x = m_2 a_{x2} = P_x$$

small angle approximation

$$\sum M_P = I_2 \ddot{\theta}_2 = \tau_2 - m_2 g \frac{l_2}{2} \cos(\theta_2)$$

$$\cos(\theta) \approx 1 \\ \sin(\theta) \approx \theta$$

$$\Rightarrow (1) \quad m_1 \ddot{y}_1 = \ddot{\theta}_1 - m_1 g - P_y, \quad m_1 \ddot{x}_1 = P_x - \ddot{\theta}_1$$

$$I_1 \ddot{\theta}_1 = \tau_1 + P_x l_1 \dot{\theta}_1 - m_1 g \frac{l_1}{2} - P_y l_1$$

$$(2) \quad m_2 \ddot{y}_2 = P_y - m_2 g, \quad m_2 \ddot{x}_2 = P_x$$

$$I_2 \ddot{\theta}_2 = \tau_2 - m_2 g \frac{l_2}{2}$$