



$$q_1 = \theta_1$$

$$q_2 = \theta_2$$

$$\bullet K = \frac{1}{2} \dot{p}^T M(q) \dot{p} = \dots$$

$$\Rightarrow M(q) = \begin{bmatrix} m_1 l_1^2 + m_2 l_1^2 + I_1 & m_2 l_1 l_2 \cos(q_2) \\ m_2 l_1 l_2 \cos(q_2) & m_2 l_2^2 + I_2 \end{bmatrix}$$

$$\Rightarrow c_{111} = \frac{1}{2} \frac{\partial m_{11}}{\partial q_1} = 0$$

$$\Rightarrow c_{121} = c_{211} = \frac{1}{2} \frac{\partial m_{11}}{\partial q_2} = 0$$

$$\Rightarrow c_{221} = \frac{\partial m_{22}}{\partial q_2} - \frac{1}{2} \frac{\partial m_{22}}{\partial q_1} = -m_2 l_1 l_2 \sin(q_2)$$

$$\Rightarrow c_{112} = \frac{\partial m_{21}}{\partial q_1} - \frac{\partial m_{11}}{\partial q_2} = 0$$

$$\Rightarrow c_{212} = c_{122} = \frac{1}{2} \frac{\partial m_{22}}{\partial q_1} = 0$$

$$\Rightarrow c_{222} = \frac{1}{2} \frac{\partial m_{22}}{\partial q_2} = 0$$

$$\bullet P = m_1 g l_1 \sin q_1 + m_2 g (l_1 \sin q_1 + l_2 \sin q_2)$$

$$\Rightarrow g_1 = (m_1 l_1 + m_2 l_1) g \cos q_1, \quad g_2 = m_2 l_2 g \cos q_2$$

$$\rightarrow \begin{cases} d_{11} \ddot{p}_1 + d_{12} \ddot{p}_2 + c_{221} \dot{p}_2^2 + g_1 = \tau_1 \\ d_{21} \ddot{p}_1 + d_{22} \ddot{p}_2 + c_{12} \dot{p}_1^2 + g_2 = \tau_2 \end{cases}$$